

HW Ch 3.1

① Find y' if

(a) $y = (4 + \sqrt[3]{x})(x^2 + 2x^3)$

solution $y = (4 + x^{\frac{1}{3}})(x^2 + 2x^3)$

$$\begin{aligned}y' &= (4 + x^{\frac{1}{3}})(x^2 + 2x^3)' + (x^2 + 2x^3)(4 + x^{\frac{1}{3}})' \\ &= (4 + x^{\frac{1}{3}})(2x + 6x^2) + (x^2 + 2x^3)(\frac{1}{3}x^{-\frac{2}{3}})\end{aligned}$$

(b) $y = \frac{1 + \sqrt{2}x^{\frac{1}{3}} + x^2}{x}$

Solution

$$\begin{aligned}y &= \frac{1 + \sqrt{2}x^{\frac{1}{3}} + x^2}{x} = \frac{1}{x} + \frac{\sqrt{2}x^{\frac{1}{3}}}{x} + \frac{x^2}{x} \\ &= x^{-1} + \sqrt{2}x^{-\frac{2}{3}} + x\end{aligned}$$

$$y' = (-1)x^{-2} + \sqrt{2}\left(-\frac{2}{3}\right)x^{-\frac{5}{3}} + 1$$

(Or use quotient rule)

② Find y'' if $y = 3x^2e^x$

solution

$$y = 3x^2e^x = (3x^2)(e^x)$$

$$\begin{aligned}y' &= (3x^2)(e^x)' + e^x(3x^2)' \\ &= 3x^2e^x + 6xe^x\end{aligned}$$

$$\begin{aligned}y'' &= (3x^2e^x)' + (6xe^x)' \\ &= 3x^2e^x + 6xe^x + 6x(e^x)' + e^x(6x)' \\ &= 3x^2e^x + 6xe^x + 6xe^x + 6e^x \\ &= 3x^2e^x + 12xe^x + 6e^x\end{aligned}$$